	Notes
Fundamentals of Programming 2	
The DFS and BFS Algorithms	
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Outline	Notes
Introduction	
The DFS Algorithm	
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Summary	
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Introduction	Notes
There are many algorithms for processing data expressed as graphs that are generally known as graph algorithms. Most of them is based on one of two	
fundamental graph traversing algorithms. Results of such algorithms are paths that start in a specified vertex and cover all vertices of a connected or strongly connected graph or end in a goal vertex. The first of those two algorithms is	
the Deep-First Search algorithm called the DFS for short. The second one is the Breadth-First Search algorithm also known as the BFS. They are described	
in this lecture in the same order as they are introduced in this slide.	
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The DFS Algorithm	
Theoretical Introduction	Notes
The ${ m DFS}$ algorithm traverses a graph starting from a specified initial vertex and visiting all vertices that are reachable from this node. If a visited vertex	
has at least one neighbour (adjacent vertex), which has not been yet visited, then this neighbour is added to a stack, as the one to be visited next. In case the visited vertex has two constants are the property of the pro	
the visited vertex has two or more unvisited neighbours, only one of them is selected. Nodes that are stored on the stack are called <i>discovered vertices</i> . The algorithm marks the current vertex as <i>visited</i> , takes a single vertex from	
the stack (provided the stack is not empty) and visits it repeating the steps described in this slide. If another algorithm is based on the DFs then it may	
process data stored in the currently visited vertex before marking it as visited.	

Theoretical Introduction

The name of the algorithm comes from the way it visits graph nodes — it always choses one of the unvisited neighbours of the current vertex and visits it as next. In other words it "goes deeper" in the graph. If the visited vertex has no unvisited neighbours (or no neighbours at all) then the DFS backtracks ("goes back") to the previous vertex and checks if there are any unvisited neighbours left. If the graph processed by the DFS is connected or strongly connected, then the algorithm will visit all its vertices. Otherwise, the DFS will visit a component (a maximal connected subgraph) that contains the initial vertex. In this case, if the objective of using the DFS is to visit all vertices of such a graph then the algorithm should be repeated for the unvisited vertices until all of them are visited.

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### The DFS Algorithm

Theoretical Introduction

The DFS algorithm can also be used for finding a path from an initial vertex to a specified  $goal\ vertex$  or a vertex that satisfies a  $goal\ condition$ . Because the DFS is a stack-based algorithm then it is easy to implement in a form of a recursive function. When this algorithm is applied to a binary tree it gives the same results as the pre-order traversal algorithm. It means that the DFS is a generalised pre-order traversal algorithm that can be applied to any graph. The time-complexity of the DFS algorithm is  $\Theta(V+E)$ .

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## The DFS Algorithm

Animation

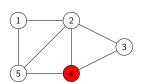
In the next slide is an animation that shows how the DFS algorithm works when applied to the undirected graph that has been presented in the previous lecture. At the top of the slide is a list of vertices which have been visited by the DFS and form a path that is the result of the algorithm. On the right is a stack, where the discovered vertices are stored. The order of visiting the neighbours is arbitrary. The vertex and the edge to be visited next are marked in red in the graph diagram. The processed vertices are marked in yellow and the vertices that have been already visited are marked in green. Because the graph is connected, the algorithm visits all its vertices in one go. There is no need to repeat it for unvisited vertices.

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#### The DFS Algorithm

Animation

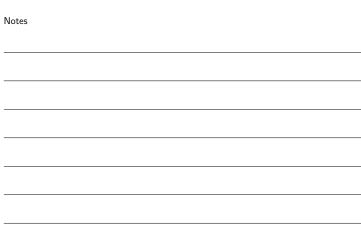
path:

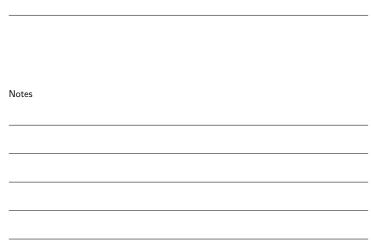


Traversing an undirected graph with the use of the DFS algorithm.

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## The DFS Algorithm Notes path: 4 (3) 4 Traversing an undirected graph with the use of the ${\ensuremath{\mathrm{DFS}}}$ algorithm. The DFS Algorithm Notes Animation path: 4 4 Traversing an undirected graph with the use of the ${\ensuremath{\mathrm{DFS}}}$ algorithm. The DFS Algorithm Notes Animation path: 4 2 (3) Traversing an undirected graph with the use of the ${\ensuremath{\mathrm{DFS}}}$ algorithm. The DFS Algorithm Notes Animation

path: 4 2

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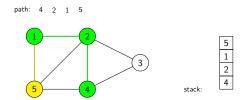
The DFS Algorithm

path: 4 2 1

1 2 1

5 4 2 1

stack:



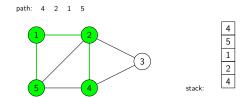
Traversing an undirected graph with the use of the  ${\ensuremath{\mathrm{DFS}}}$  algorithm.

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Notes

## The DFS Algorithm

Animation

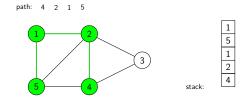


Traversing an undirected graph with the use of the  ${\ensuremath{\mathrm{DFS}}}$  algorithm.

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## The DFS Algorithm

Animation

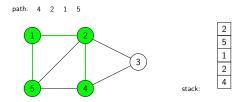


Traversing an undirected graph with the use of the  ${\ensuremath{\mathrm{DFS}}}$  algorithm.

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## The DFS Algorithm

Animation

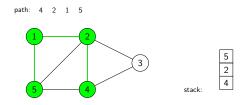


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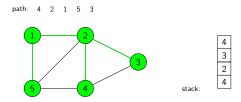
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The DFS Algorithm Animation

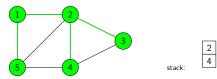


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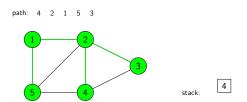
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## The DFS Algorithm Notes path: 4 2 1 5 3 2 Traversing an undirected graph with the use of the ${\ensuremath{\mathrm{DFS}}}$ algorithm. The DFS Algorithm Notes Animation path: 4 2 1 5 3 Traversing an undirected graph with the use of the ${\ensuremath{\mathrm{DFS}}}$ algorithm. The DFS Algorithm Notes Animation path: 4 2 1 5 3 2 4 Traversing an undirected graph with the use of the ${\ensuremath{\mathrm{DFS}}}$ algorithm. The DFS Algorithm Notes Animation path: 4 2 1 5 3

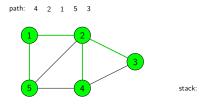


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Traversing an undirected graph with the use of the DFS algorithm.

Animation



Traversing an undirected graph with the use of the DFS algorithm.

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Notes

#### The DFS Algorithm — Implementation

Next slides show a modified version of the program presented in the previous lecture which traverses an undirected graph using the  ${\tt DFS}$  algorithm. The input for this algorithm is the graph adjacency list which is the result of converting the adjacency matrix. Because the graph is connected, the  ${\tt DFS}$  visits all its vertices in one go, but the program is also prepared for processing graphs which are not connected.

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#### The DFS Algorithm — Implementation

Adjacency Matrix and Base Type of Adjacency List

```
#include<stdio.h>
#include<stdibi.h>
#include<stdibi.h>
#include<stdibi.h>

typedef int matrix[5][5];

const matrix adjacency_matrix = {{0,1,0,0,1},
{0,1,1,1,1},
{0,1,0,1,0,1},
{0,1,0,1,0,1},
{1,1,0,1,0,1};

struct vertex {
    int vertex_number;
    bool visited;
    struct vertex *next, *down;
} *start_vertex;
```

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#### The DFS Algorithm — Implementation

Adjacency Matrix and Base Type of Adjacency List

Two new elements have been added to the beginning of the program. The first one is the preprocessor directive that includes the stdbool.h header file. The second one is a field in the adjacency list base type, called visited. The data type of this field is bool. The value of the field has a meaning only in the list of all graph vertices — the "vertical" list, which is a part of the adjacency list. If the vertex represented by the element of this list has been already visited then the value of its visited field is true, otherwise it is false.

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The Queue Base Type and the Queue Pointers Structure

```
struct fifo_node {
int vertex_number;
struct fifo_node *next;
};

struct fifo_pointers {
struct fifo_pointers {
struct fifo_node *head, *tail;
} } path;
```

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#### The DFS Algorithm — Implementation

The Queue Base Type and the Queue Pointers Structure

In the previous slide are presented definitions of a FIFO queue element base type and a structure that stores the head and tail pointers of that queue. A global variable of the fifo\_pointers type, named path, is also declared in this part of the program (8th line). The queue is used for storing the path that is the result of the DFS, hence each of its elements stores the number of a visited vertex.

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## The DFS Algorithm — Implementation

The enqueue() Function

```
void enqueue(struct fifo_pointers *fifo, int vertex_number)

{
    struct fifo_node *new_node =
        (struct fifo_node *)malloc(sizeof(struct fifo_node));
    if(new_node) {
        new_node->vertex_number = vertex_number;
        new_node->next = NULL;
    if(fifo->head==NULL)
        fifo->head = fifo->tail = new_node;
    else {
        fifo->tail->next=new_node;
        fifo->tail=new_node;
    }
} else
fprintf(stderr,"No new element was created!\n");
}
```

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#### The DFS Algorithm — Implementation

The enqueue() Function

In the previous slide is shown a definition of the enqueue() function, which adds an element to a  ${\rm FIFO}$  queue. Please refer to the lecture on queues for more detailed description of this function.

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The dequeue() Function

```
void dequeue(struct fifo_pointers *fifo)
{
    if(fifo->head) {
        struct fifo_node *tmp = fifo->head->next;
        free(fifo->head);
        fifo->head=tmp;
        if(tmp==NULL)
        fifo->tail = NULL;
}
```

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### The DFS Algorithm — Implementation

The dequeue() Function

The main difference between the dequeue() function presented in the previous slide and its equivalent presented in the lecture on queues is that the former returns no value, but only removes a single element from the head of the FIFO queue.

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## The DFS Algorithm — Implementation

The remove\_queue() Function

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#### The DFS Algorithm — Implementation

The remove\_queue() Function

The remove\_queue() function calls in the while loop the dequeue() function to delete the FIFO queue. As an argument it takes the address of the queue pointers structure. It doesn't return any value. The while loop stops when the head pointer has a value of NULL.

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The print\_path() Function

```
void print_path(struct fifo_pointers fifo)
{
    while(fifo.head) {
        printf("",'d ",fifo.head->vertex_number);
        fifo.head = fifo.head->next;
    }
    puts("");
}
```

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Notes

### The DFS Algorithm — Implementation

The print\_path() Function

The print\_path() function is basically the print\_queue() function modified to print the content of the FIFO queue storing the path created by the DFS algorithm.

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## The DFS Algorithm — Implementation

The create\_vertical\_list() Function

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## The DFS Algorithm — Implementation

The create\_vertical\_list() Function

The create\_vertical\_list() function differs from its equivalent from the previous lecture only in that it initializes (10th line) the visited field of each node representing a vertex in the list of all vertices.

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The convert\_matrix\_to\_list() Function

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### The DFS Algorithm — Implementation

The convert\_matrix\_to\_list() Function

The function that converts an adjacency matrix into an adjacency list also differs by only one detail from its equivalent from the previous lecture. This detail is the initialisation of the visited field (15th line) of each newly created node of the neighbours lists ("vertical" lists in the adjacency list).

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## The DFS Algorithm — Implementation

The print\_adjacency\_list() Function

```
void print_adjacency_list(struct vertex *start_vertex)

this is the printf("",3d:",start_vertex_vertex_number);

struct vertex *horizontal_pointer = start_vertex_number);

while(horizontal_pointer) {
 printf("",3d",horizontal_pointer_vertex_number);
 horizontal_pointer = horizontal_pointer_next;
}

start_vertex = start_vertex_down;
puts("");
}
```

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## The DFS Algorithm — Implementation

The  $print_adjacency_list()$  Function

The print\_adjacency\_list() function is implemented in exactly the same way as its equivalent from the previous lecture.

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The remove\_adjacency\_list() Function

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## The DFS Algorithm — Implementation

The remove\_adjacency\_list() Function

The  $remove\_adjacency\_list()$  function is also implemented in the same way as its equivalent from the previous lecture.

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## The DFS Algorithm — Implementation

The find\_vertex() Function

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#### The DFS Algorithm — Implementation

The find\_vertex() Function

The find\_vertex() function is a helper subroutine for the function that implements the DFS algorithm. Its task is to locate a node in the list of all vertices (the "vertical" list) that represents a vertex of a specified number. It takes as arguments the address of the adjacency list starting node and the number of the sought vertex. The function traverses the list of all vertices using the while loop and the start\_vertex parameter (lines no. 4–6) and it checks if the node currently pointed by this parameter stores the sought number. If not, it advances to the next element of the list, otherwise the loop stops and the function returns the address of the located node that represents the sought vertex. The function returns the NULL value when its first argument is an empty pointer or the second argument is a number of a nonexistent vertex.

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The has\_not\_been\_visited() Function

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#### The DFS Algorithm — Implementation

The has\_not\_been\_visited() Function

The has\_not\_been\_visited() function checks if a specified vertex is unvisited. It takes two arguments: the address of the adjacency list starting node and the address of the node representing the verified vertex in the list of neighbours (one of the "horizontal" lists) of the currently visited vertex. The has\_not\_been\_visited() function invokes the find\_vertex() function to locate the node representing the verified vertex in the list of all vertices (the "vertical" list). The latter function returns a pointer to the sought element, which is immediately dereferenced¹ (5th line) to get the value of the visited field of the verified vertex. The has\_not\_been\_visited() function returns a negated value of that field.

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#### The DFS Algorithm — Implementation

The dfs() Function

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#### The DFS Algorithm — Implementation

The dfs() Function

The dfs() function, as its name suggests, implements the DFS algorithm. It doesn't return any value and takes three arguments. The first one is the address of the adjacency list starting node. The second one is the address of the initial vertex for the DFS algorithm. The last argument is the address of the FIFO queue pointers structure. The queue is used for storing the path created by the function. In the 4th line the function verifies if the addresses of vertices passed by its parameters are not NULL. If so, then it adds to the FIFO queue a new element that stores the number of the vertex that is represented by a node pointed by the vertex parameter (5th line). Next, the function marks the vertex as visited by storing the true value in the visited field (6th line). Then it performs the while loop. Inside that loop the function takes the address stored in the next field of a node pointed by the vertex pointer and assigns it to that pointer (8th line).

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¹It is not the best idea — the find\_vertex() function may return the NULL value.

The dfs() Function

If the address is not NULL, then it means that the currently visited vertex has at least one neighbour and now the vertex pointer points to a node in the neighbours list that represents the first of them. In lines no. 9 and no. 10 the dfs() function verifies the existence of that vertex and if it is unvisited. If both conditions are met then the function invokes itself recursively for the neighbour vertex. This time as the second argument it takes the result of the find\_vertex() function which returns the address of the node representing the neighbour vertex in the list of all vertices of the graph (the "vertical" list). After the dfs() function returns from the recursive call a next iteration of the while loop is performed. If another unvisited neighbour of the current vertex exists then the dfs() function calls itself recursively again, but this time for that neighbour vertex.

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#### The DFS Algorithm — Implementation

The visit\_all\_vertexes() Function

```
void visit_all_vertexes(struct vertex *start_vertex)
{
    struct vertex *vertex = start_vertex;
    while(vertex) {
        if(!vertex->visited) {
            struct fifo_pointers path;
            path.head = path.tail = NULL;
            dfs(start_vertex,vertex,&path);
            print_path(path);
            remove_queue(&path);
        }
        vertex = vertex->down;
}
```

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#### The DFS Algorithm — Implementation

The visit\_all\_vertexes() Function

The visit\_all\_vertexes() function is invoked after the dfs() function exits. It verifies if all the vertices of the graph have been visited and it calls the dfs() function for those of them that haven't been. The function returns no value, but takes one argument which is the address of the adjacency list starting node. In the 3rd line a local pointer named vertex is declared and initialized with the address stored in the start\_vertex parameter. Although the function could used the start\_vertex parameter for traversing the list of all vertices, without any consequences for the rest of the program, since its argument is passed by value, it is necessary to use another pointer for that purpose, because the address of the adjacency list starting node is used in another part of the function.

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#### The DFS Algorithm — Implementation

The visit\_all\_vertexes() Function

In the while loop the function traverses the list of all vertices of the graph (the "vertical" list) using the vertex pointer and checks if any of them has not been yet visited (line no. 5). If so, then in the 8th line the dfs() function is invoked for that unvisited vertex. The address of the FIFO queue pointers structure declared in the 6th line and initialised in the 7th line is passed as the last argument of the dfs() function. In other words the visit\_all\_vertexes() function uses its own local FIFO queue. After the dfs() function exits the content of the queue is displayed on the screen and the queue is deleted, allowing the queue pointers structure to be used again for creating another instance of the queue in case some unvisited vertices are still left in the graph. The while loop stops after each node in the list of all vertices has been verified, which assures that the whole graph is traversed.

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The main() Function

```
int main(void)
{
    start_vertex = convert_matrix_to_list(adjacency_matrix);
    if(start_vertex) {
        print_adjacency_list(start_vertex);
        puts("Please enter the number of the initial vertex:");
        int vertex_number = 0;
        scarn("%", kvertex_number);
        dfs(start_vertex,find_vertex(start_vertex_vertex_number), &path);
        puts("The DFS algorithm result:");
        print_path(path);
        remove_queue(&path);
        visit_all_vertexes(start_vertex);
    }
    remove_adjacency_list(&start_vertex);
    }
    return 0;
}
```

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Notes

#### The DFS Algorithm — Implementation

The main() Function

In the 6th line the main() function displays a message asking the user to enter the number of the initial vertex for the DFS algorithm. The number is stored in a local variable named vertex\_number (8th line). Next, the dfs() function is called. The second argument of that function — the address of the node representing the initial vertex in the list of all vertices — is returned by the find\_vertex() function. The path returned by the dfs() function is displayed on the screen (lines no. 10 and 11) and the program deletes the queue that stores the path (12th line). In the 13th line the main() function calls the visit\_all\_vertexes() function to visit all the unvisited vertices of the graph. The rest of the main() function is the same as in the program presented in the previous lecture.

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#### The BFS Algorithm

Theoretical Introduction

The BFS algorithm, just like the DFS algorithm, traverses a graph. The main difference between those two algorithms is that the BFS uses a FIFO queue instead of a stack to store the discovered vertices. When visiting a vertex the algorithm adds all its unvisited neighbours to this queue. After marking the current vertex as visited the BFS algorithm removes and visits the first discovered vertex from the head of the queue. All neighbours of every vertex are visited before any other vertices, hence the name of this algorithm: Breadth-First Search. The algorithm is usually implemented in a form of an iterative function. Its time-complexity is  ${\cal O}(V+E)$ .

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#### The BFS Algorithm

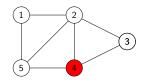
Animation

In the next slide is an animation that shows how the BFS algorithm works when it is applied for an undirected graph — it is the same graph as in the case of the DFS algorithm. In the animation the FIFO queue is used instead of the stack. It is shown at the bottom of the slide. All other elements of the animation are the same as for the DFS algorithm.

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Animation

path:



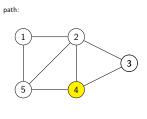
FIFO queue:

Traversing an undirected graph with the use of the  ${\ensuremath{\mathrm{BFS}}}$  algorithm.

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## The BFS Algorithm

Animation



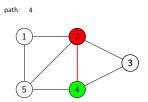
FIFO queue: 4

Traversing an undirected graph with the use of the  ${\ensuremath{\mathrm{BFS}}}$  algorithm.

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## The BFS Algorithm

Animation

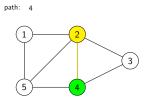


FIFO queue:

Traversing an undirected graph with the use of the BFS algorithm.

The BFS Algorithm

Animation



FIFO queue: 2

Traversing an undirected graph with the use of the  ${\ensuremath{\mathrm{BFS}}}$  algorithm.

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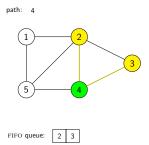
path: 4

Traversing an undirected graph with the use of the  ${\ensuremath{\mathrm{BFS}}}$  algorithm.

Notes

## The BFS Algorithm

Animation

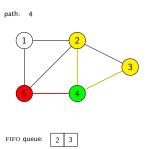


Traversing an undirected graph with the use of the  ${\ensuremath{\mathrm{BFS}}}$  algorithm.

Notes

## The BFS Algorithm

Animation

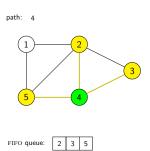


Traversing an undirected graph with the use of the BFS algorithm.

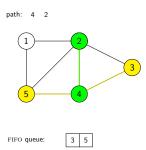
Notes

## The BFS Algorithm

Animation



Animation

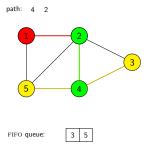


Traversing an undirected graph with the use of the  ${\ensuremath{\mathrm{BFS}}}$  algorithm.

Notes

## The BFS Algorithm

Animation

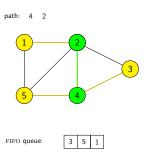


Traversing an undirected graph with the use of the  ${\ensuremath{\mathrm{BFS}}}$  algorithm.

Notes

## The BFS Algorithm

Animation

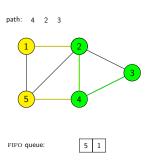


Traversing an undirected graph with the use of the  ${\ensuremath{\mathrm{BFS}}}$  algorithm.

Notes

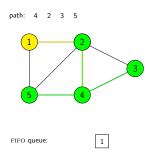
## The BFS Algorithm

Animation



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Animation



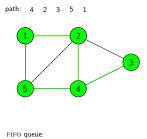
Traversing an undirected graph with the use of the  ${\ensuremath{\mathrm{BFS}}}$  algorithm.

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## The BFS Algorithm

Animation



Traversing an undirected graph with the use of the BFS algorithm.

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## The BFS Algorithm — Implementation

Next slides present the program demonstrated earlier, but this time it uses the  $_{\rm BFS}$  algorithm instead of the  $_{\rm DFS}$  for traversing a graph. Only those elements that have been modified are described.

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## The BFS Algorithm — Implementation

Adjacency Matrix and Base Type of Adjacency List

1	#include <stdio.h></stdio.h>
2	#include <stdlib.h></stdlib.h>
3	#include <stdbool.h></stdbool.h>
4	
5	<pre>typedef int matrix[5][5];</pre>
6	
7	<pre>const matrix adjacency_matrix = {{0,1,0,0,1},</pre>
8	{1,0,1,1,1},
9	{0,1,0,1,0},
10	{0,1,1,0,1},
11	{1,1,0,1,0}}
12	
13	struct vertex
14	{
15	<pre>int vertex_number;</pre>
16	<pre>bool visited;</pre>
17	struct vertex *next, *down;
18	<pre>} *start_vertex;</pre>

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The Queue Base Type and the Queue Pointers Structure

```
struct fifo_node

int vertex_number;

struct fifo_node *next;

};

struct fifo_pointers

struct fifo_node *head, *tail;

path_fifo, discovered_fifo;
```

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#### The BFS Algorithm — Implementation

The Queue Base Type and the Queue Pointers Structure

Please notice, that an additional variable, named discovered\_fifo, is declared in this part of code. It is a structure of pointers for the queue of discovered vertices.

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## The BFS Algorithm — Implementation

The enqueue() Function

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## The BFS Algorithm — Implementation

The dequeue() Function

```
int dequeue(struct fifo_pointers *fifo)
{
    int vertex_number = -1;
    if(fifo->head) {
        struct fifo_node *tmp = fifo->head->next;
        vertex_number = fifo->head->vertex_number;
        free(fifo->head);
        fifo->head=tmp;
        if(tmp==NULL)
            fifo->tail = NULL;
}
return vertex_number;
}
```

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## The BFS Algorithm — Implementation Notes The dequeue() Function The dequeue() function, unlike its equivalent from the earlier program, returns the number of the vertex represented by the element removed from the queue. If the queue is empty the function returns $\ensuremath{^{\text{-}}} 1.$ The BFS Algorithm — Implementation Notes The remove\_queue() Function void remove\_queue(struct fifo\_pointers \*fifo) while(fifo->head) dequeue(fifo); The BFS Algorithm — Implementation Notes The print\_path() Function void print\_path(struct fifo\_pointers fifo) while(fifo.head) { printf("%d ",fifo.head->vertex\_number); fifo.head = fifo.head->next; puts(""); The BFS Algorithm — Implementation Notes The create\_vertical\_list() Function void create\_vertical\_list(struct vertex \*\*start\_vertex, const matrix adjacency\_matrix) for(i=0; i<sizeof(matrix)/sizeof(\*adjacency\_matrix); i++) { \*start\_vertex = (struct vertex \*)</pre> malloc(sizeof(struct vertex)); if(\*start\_vertex) { (\*start\_vertex)->vertex\_number = i+1; (\*start\_vertex)->visited = false; (\*start\_vertex)->down = (\*start\_vertex)->next = NULL; start\_vertex = &(\*start\_vertex)->down; 14 15 } }

The convert\_matrix\_to\_list() Function

```
1 struct vertex *convert_matrix_to_list(const matrix adjacency_matrix)
2 {
2 struct vertex *start_vertex * NULL;
3 creat_vertical_list(start_vertex_adjacency_matrix);
5 if(start_vertex) {
5 if(start_vertex) {
6 struct vertex * hebrizontal_pointer * NULL, * vertical_pointer * NULL;
8 horizontal_pointer * vertical_pointer * start_vertex;
9 is i_j;
9 is i_j;
10 is i_j;
11 if(adjacency_matrix[i]);
12 if(adjacency_matrix[i]);
13 if(adjacency_matrix[i]);
14 is it(adjacency_matrix[i]);
15 is inv_vertex * (struct vertex *)malloc(sizeof(struct vertex));
16 is inv_vertex_vertex * (struct vertex *)malloc(sizeof(struct vertex));
17 is new_vertex_vertex * is new_vertex_lost
18 is new_vertex_vertex * is new_vertex_lost
19 is new_vertex_vertex * is new_vertex_lost
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12 is new_vertex_lost
13 is new_vertex_lost
14 is new_vertex_lost
15 is new_vertex_lost
16 is new_vertex_lost
17 is new_vertex_lost
18 is new_v
```

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### The BFS Algorithm — Implementation

The print\_adjacency\_list() Function

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## The BFS Algorithm — Implementation

The  $remove\_adjacency\_list()$  Function

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## The BFS Algorithm — Implementation

The find\_vertex() Function

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The has\_not\_been\_visited() Function

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#### The BFS Algorithm — Implementation

The bfs() Function

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## The BFS Algorithm — Implementation

The bfs() Function

The bfs() function implements the BFS graph traversal algorithm. It returns no value but takes four arguments — an address of the adjacency list starting node, an address of the initial vertex for the BFS algorithm, an address of the pointers structure for the queue where the path created by the algorithm will be stored and an address for another pointers structure, but this time for the queue which will store the discovered vertices. In the 4th line the function verifies if the first two addresses passed by its parameters are not NULL. If so, it adds to the discovered\_fifo queue a new element storing the number of the vertex also stored in the node pointed by the vertex parameter (5th line) and starts the outer while loop, which is repeated until the queue of discovered vertices is empty (6th line).

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#### The BFS Algorithm — Implementation

The bfs() Function

Inside this loop the bfs() function removes the first element from the discovered\_fifo queue (7th line) and assigns the vertex number stored in that element to the vertex\_number variable, which is then used by the find\_vertex() function to find the address of the node representing that vertex in the list of all vertices. This address is assigned to the vertex pointer. In the 9th line the function checks if the vertex is unvisited. If so, then it assigns the address stored in the next field of the node pointed by the vertex variable to the next\_vertex pointer. If after the assignment the value of this pointer is not NULL then it means that the vertex has a nonempty list of its neighbours and that the next\_vertex pointer points to the first element of this list. Inside the inner while loop (lines no. 11-14) the bfs() function traverses that list, gets the vertex numbers stored in its elements and adds them to the discovered\_fifo queue.

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The bfs() Function

When the inner loop stops the bfs() function marks the current vertex (pointed by the vertex pointer) as visited and stores its number in the path\_fifo queue. The function exits when all vertices reachable from the initial vertex are visited. The result of this function is the path stored in the path\_fifo queue.

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#### The BFS Algorithm — Implementation

The visit\_all\_vertexes() Function

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## The BFS Algorithm — Implementation

The visit\_all\_vertexes() Function

The visit\_all\_vertexes() function differs from its equivalent from the previous program in that it invokes the bfs() function instead of the dfs() function (10th line) and it uses two FIFO queues instead of one. The pointers structure of the second queue is declared in the 7th line and initialised in lines no. 8 and no. 9. This queue is used by the bfs() function for storing the discovered vertices and then it is deleted in the 13th line.

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#### The BFS Algorithm — Implementation

The main() Function

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The BFS Algorithm — Implementation  The main() Function		Notes
There are two changes in the main() function. First of all it calls the bfs() function instead of the dfs() function. It also declares and initializes the		
discovered_fifo queue pointers structure, which is then used by the bfs() function. The function that deletes the discovered vertices queue is called in		
the 14th line, although if the bfs() function completes its job successfully then this queue should already be empty.		
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Summary		Notes
The BFS and DFS algorithms can be applied either to undirected or directed graphs and it doesn't matter if those graphs are connected, strongly connected		
or disconnected. The two algorithms are the basis of many other graph algorithms. Among them is a family of heuristic graph traversal algorithms known		
as Best-First Search algorithms. One of them is the $A^*$ algorithm. Initially the BFS and DFS algorithms were used in the Artificial Intelligence, but nowadays they are applied in many other branches of Computer Science.		
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Questions		Notes
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THE END		Notes
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Thank You For Your Attention!		